



I'm not robot



**I am not robot!**

The graph of  $f$  is concave up on  $I$  if  $f$  increases on  $I$ . The graph of  $f$  is concave down on  $I$  if  $f$  decreases on  $I$ . Points that join arcs of opposite concavity are points of inflection. In Chapter 3, you saw that the second derivative of a function has applications in problems involving velocity and acceleration.

**Section Concavity and Points of Inflection**

**CONCAVE DOWN** . . . Of particular interest are points at which the concavity changes from up to down or down to up; such points are called inflection points. We now know how to determine where a function is increasing or decreasing. (b) Find intervals on which the graph of  $f$  is concave up and concave down. If  $(a, f(a))$  is a point of inflection, then either  $f''(a) = 0$  or  $f''(a)$  does not exist. Please note that the converse of the above statement is NOT true.

**CONCAVITY AND INFLECTION POINTS**

A function  $f$  is concave down on an interval  $I$  if the graph of  $f$  lies under its tangent lines on the interval: ' @ @'. How do we find the points of inflection? This notion is called the concavity of the function.

**CONCAVITY AND INFLECTION POINTS Example**

The first derivative of a certain function  $f(x)$  is  $f'(x) = x^2 - 2x$ .

(a) Find intervals on which  $f$  is increasing and decreasing. Find intervals on which the graph of  $f$  is concave up and concave down. The graph of  $f$  is concave up on  $I$  if  $f'$  increases on  $I$ . The graph of  $f$  is concave down on  $I$  if  $f'$  decreases on  $I$ . Points that join arcs of opposite concavity are points of inflection. Find the  $x$  coordinate of the relative extrema and inflection points of  $f$ . However, there is another issue to consider regarding the shape of the graph of a function. If  $(a, f(a))$  is a point of inflection, then either  $f''(a) = 0$  or  $f''(a)$  does not exist.

**Definition.** How do we find the points of inflection? If the concavity changes.

The point  $(a, f(a))$  is a point of inflection if the graph of  $f$  changes concavity at  $x = a$ . Set the Second Derivative equal to zero and solve. The first derivative of a certain function  $f(x)$  is  $f'(x) = x^2 - 2x$ .

**CONCAVITY AND INFLECTION POINTS Geometrically,** inflection points occur at "twists" on a graph, as indicated in the following.

**CONCAVITY AND INFLECTION POINTS.** (c) Find the  $x$  coordinate of the relative extrema and inflection points of  $f$ .

**Section Concavity and Points of Inflection**

In Chapter 3, you saw that the second derivative of a function has applications in problems involving velocity and acceleration or in general rates-of-change problems. Of particular interest are points at which the concavity changes from up to down or down to up; such points are called inflection points. If the concavity changes from up to down at  $(x=a)$ ,  $f''(x)$  changes from positive to the left of  $(a)$  to negative to the right of  $(a)$ , and usually  $f''(a) = 0$ .

The point  $(a, f(a))$  is a point of inflection if the graph of  $f$  changes concavity at  $x = a$ .

**Example.** Example Find the points of inflection and determine the concavity of  $f$ .

**Definition.** If the graph curves, does it curve upward or curve downward? Determine whether the Second Derivative Test applies.

If a function has inflection points, then they will exist at values of  $x$  at which or. An inflection point of  $f$  (or point of inflection, if procedure for determining the concavity of a graph and locating its inflection points. Find the Second Derivative of the function,  $f$ . Determine the intervals on which  $f$  increases and the intervals on which  $f$  decreases.

Points on the graph of a function at which the concavity changes from up to down or vice versa.